## Self-energy renormalization around the flux phase in the *t-J* model: Possible implications in underdoped cuprates

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The flux phase predicted by the *t-J* model in the large-*N* limit exhibits features that make it a candidate for describing the pseudogap regime of cuprates. However, certain properties, such as, for instance, the prediction of well-defined quasiparticle peaks, speak against this scenario. We have addressed these issues by computing self-energy renormalizations in the vicinity of flux phase. The calculated spectral functions show features similar to those observed in experiments. At low doping, near the flux phase, the spectral functions are anisotropic on the Fermi surface and very incoherent near the hot spots. The temperature and doping evolution of self-energy and spectral functions are discussed and compared with the experiment.

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The pseudogap (PG) phase of high- $T_c$  cuprates presents unusual properties in clear contrast to those expected for conventional metals<sup>1</sup> and, in spite of the many scenarios proposed, the problem remains open. A well-known phenomenological theory is the d-CDW (where CDW denotes charge-density wave),<sup>2</sup> in which a normal state (NS) gap was proposed. Interestingly, d-CDW is closely related to the flux phase (FP), which was formerly predicted in the context of the t-J model.<sup>3</sup> In both scenarios, the PG coexists and competes with superconductivity, is complex, and shows d-wave symmetry. FP was also studied by means of different analytical and numerical methods.<sup>4–7</sup> In the mean-field approximation of the t-J model, below a characteristic temperature  $T^*$ . a d-wave NS gap opens on the Fermi surface (FS) near the hot spots  $[\mathbf{k} \cong (0, \pi)]$ . This leads to pockets with low spectral weight intensity in the outer section.<sup>8</sup> Thus, these pockets resemble the arcs observed in angle-resolved photoelectron spectroscopy (ARPES) experiments.<sup>9</sup> Furthermore, recent progress on the t-J model shows that the competition between FP and superconductivity leads to a phase diagram qualitatively similar to that observed in cuprates.<sup>5</sup> Raman and tunneling spectroscopy results show similarities with the experiment. <sup>10</sup> Very recent ARPES, <sup>11</sup> Raman, <sup>12</sup> specific heat, <sup>13</sup> and femtosecond optical pulse <sup>14</sup> experiments together with some theoretical developments<sup>15</sup> support the competing two-gap scenario. From the above reasons, FP may be considered as a good candidate for describing the PG region. Nevertheless, there are some drawbacks to be addressed. While in the FP scenario a true phase transition occurs at  $T^*$ , many experiments show a smooth behavior as a function of temperature. 16 In addition, well-defined quasiparticle (QP) peaks are predicted everywhere on the Brillouin zone, above and below  $T^*$ , while experiments show that the QP exists only near the nodal direction.<sup>17</sup> Near hot spots, coherent peaks are observed neither below nor above the PG temperature in apparent contradiction with the FP picture. On the other hand, the PG observed in ARPES, consistent with tunneling experiments, 18 seems to be filling up but is not closing, <sup>19</sup> leading to a smooth evolution of spectral properties.

In spite of the above objections, we will assume the point

of view that the basic physics of cuprates is contained in the t-J model (see Ref. 20 for discussions). Moreover, to address the above discussion, it is necessary to perform a controllable self-energy and spectral function calculation beyond mean field. Recently, a large-N approach for the t-J model based on the path integral representation for X operators was proposed.<sup>6</sup> At the mean-field level, the approach of Ref. 6 agrees with slave boson<sup>3,4</sup> and the approach of Ref. 5. Additionally, it can be easily applied beyond mean field, allowing the calculation of self-energy and spectral functions.<sup>21</sup> In this Brief Report, we discuss spectral functions and self-energy calculations in the NS in the vicinity to the FP instability. We have found that the spectral functions and the corresponding self-energies are very anisotropic on the FS, leading to a well-defined QP near the nodal direction and very incoherent features near the hot spots.

We study the two-dimensional t-J model with hopping tand Heisenberg coupling J/t=0.3 between nearest-neighbor sites on the square lattice.<sup>22</sup> In the following, energy is in units of t. Using the formulation described in Ref. 6, the mean-field homogeneous Fermi liquid (HFL) becomes unstable when the static ( $\omega$ =0) flux susceptibility  $\chi_{flux}(\mathbf{q},\omega)$  $=(\frac{\delta}{2})^2[(8/J)\Delta^2 - \Pi(\mathbf{q},\omega)]^{-1}$  diverges.  $\Pi(\mathbf{q},\omega)$  is an electronic bubble calculated with a form factor  $\gamma(\mathbf{q}, \mathbf{k}) = 2\Delta [\sin(k_x - q_x/2) - \sin(k_y - q_y/2)].^{6,21,23}$ (For the definition of  $\Delta$ , see below.) In Fig. 1(a), the phase diagram in the doping-temperature  $(\delta - T)$  plane is presented, where  $T^*$ indicates the FP instability onset. At T=0, a phase transition occurs at the critical doping  $\delta_c \cong 0.12$  for the incommensurate critical vector  $\mathbf{q}_c \cong (1,0.86)\pi$  near  $(\pi,\pi)$ . At finite T, the instability is commensurate  $[\mathbf{q}_c = (\pi, \pi)]$ . Therefore, since the instability takes place at, or close to,  $(\pi, \pi)$ , the form factor  $\gamma(\mathbf{q}, \mathbf{k})$  transforms to  $\sim [\cos(k_x) - \cos(k_y)]$ , which indicates the d-wave character of the FP. Since  $T^*$  falls abruptly to zero at  $\delta_c$ , <sup>24</sup> we associate the FP with the scenario discussed in Fig. 1(a) of Ref. 16. In Fig. 1(b), we have plotted Im  $\chi_{flux}(\mathbf{q}=(\pi,\pi),\omega)$  at T=0, which shows that when  $\delta \rightarrow \delta_c$ , a low-energy d-wave flux mode becomes soft, accumulating large spectral weight. This soft mode reaches  $\omega = 0$  at  $\delta = \delta_c$ , freezing the FP.

For studying the soft mode influence on one-electron

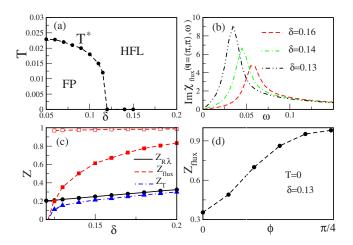


FIG. 1. (Color online) (a) Large-N t-J model phase diagram in the  $\delta$ -T plane. (b) Softening of the d-wave flux mode for several  $\delta$  values approaching  $\delta_c \cong 0.12$ . (c) QP weight Z for  $\Sigma_{R\lambda}$  (black circles),  $\Sigma_{flux}$  (red squares), and  $\Sigma_T$  (blue triangles). (d)  $Z_{flux}$  versus the FS angle  $\phi$  for  $\delta$ =0.13.

spectral properties, we calculate self-energy renormalizations in the NS in the vicinity of  $T^*$ . The inclusion of the superconducting ground state in the calculation does not change significantly the FP region (see Refs. 5 and 10). After collecting all contributions in  $\mathcal{O}(1/N)$ , the self-energy can be written as<sup>21</sup> [in  $\mathcal{O}(1/N)$ , the inclusion of self-energy corrections in the calculation of electronic bubbles is not necessary]

$$\operatorname{Im} \Sigma_{T}(\mathbf{k}, \omega) = \operatorname{Im} \Sigma_{R\lambda}(\mathbf{k}, \omega) + \operatorname{Im} \Sigma_{flux}(\mathbf{k}, \omega), \tag{1}$$

where

$$\operatorname{Im} \Sigma_{R\lambda}(\mathbf{k}, \omega) = -\frac{1}{N_s} \sum_{\mathbf{q}} \left\{ \Omega^2 \operatorname{Im}[D_{RR}(\mathbf{q}, \omega - \epsilon_{k-q})] + 2\Omega \operatorname{Im}[D_{\lambda R}(\mathbf{q}, \omega - \epsilon_{k-q})] + \operatorname{Im}[D_{\lambda \lambda}(\mathbf{q}, \omega - \epsilon_{k-q})] \right\} \times [n_F(-\epsilon_{k-q}) + n_B(\omega - \epsilon_{k-q})]$$
(2)

and

Im 
$$\Sigma_{flux}(\mathbf{k}, \omega) = -\frac{1}{N_s} \sum_{\mathbf{q}} \gamma^2(\mathbf{q}, \mathbf{k}) \text{Im } \chi_{flux}(\mathbf{q}, \omega - \epsilon_{k-q})$$

$$\times [n_F(-\epsilon_{k-q}) + n_B(\omega - \epsilon_{k-q})]. \tag{3}$$

In the above expressions,  $\Omega = (\varepsilon_{k-q} + \omega + \mu)/2$ ,  $\varepsilon_k = (t\delta + \Delta)[\cos(k_x) + \cos(k_y)]$  is the mean-field electronic dispersion,  $\epsilon_k = \varepsilon_k - \mu$ , and  $\Delta = \frac{J}{2N_s} \Sigma_k \cos(k_x) n_F(\epsilon_k)$ .  $n_B (n_F)$  is the Bose (Fermi) factor,  $\mu$  is the chemical potential, and  $N_s$  is the number of sites.  $\Sigma_{R\lambda}$  corresponds to the charge  $(\delta R)$  sector, nondouble occupancy  $(\delta \lambda)$  sector, and the mixing of both. Since for J = 0.3 there is no important influence of J contributions in  $\Sigma_{R\lambda}$ , then  $\Sigma_{R\lambda}$  is close to the self-energy for J = 0. Instead,  $\Sigma_{flux}$  is dominated by J. The explicit expressions of  $D_{RR}$ ,  $D_{\lambda R}$ , and  $D_{\lambda \lambda}$  are given in Ref. 21.

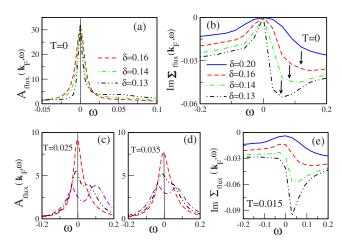


FIG. 2. (Color online) (a) T=0 spectral functions at the antinodal  $k_F$  for several doping values approaching  $\delta_c$ . A broadening  $\eta=0.01$  was used in the calculation. The vertical line marks the Fermi level. (b) T=0 flux scattering rate for several  $\delta$  values at the antinodal  $k_F$ . [(c) and (d)] Spectral functions at the antinodal  $k_F$  for T=0.025 and T=0.035, respectively, for  $\delta=0.16$  (red dashed line),  $\delta=0.13$  (black double-dotted-dashed line), and  $\delta=0.10$  (violet double-dashed-dotted line). (e) The same as in (b), but for T=0.015.

In Fig. 1(c), we have plotted the QP weight  $Z=1/(1-\partial \operatorname{Re} \Sigma/\partial \omega)$  vs  $\delta$  for each self-energy contribution.  $Z_{R\lambda}$  (black circles) are results at the Fermi crossing momentum in the (0,0)- $(0,\pi)$  direction (antinodal  $k_F$ ).  $Z_{R\lambda}$  decreases (linearly) with decreasing doping  $(Z_{R\lambda} \rightarrow 0$  when  $\delta \rightarrow 0$ ). Due to the fact that  $\Sigma_{R\lambda}$  is very isotropic on the FS, results for  $Z_{R\lambda}$  at the Fermi crossing momentum in the nodal direction (nodal  $k_F$ ) are very similar to those for the antinodal  $k_F$ . In contrast,  $Z_{flux}$  (red squares) is strongly anisotropic on the FS. For nodal  $k_F$  (open red squares),  $Z_{flux} \sim 1$ , which means that  $\Sigma_{flux}$  has no important contribution near the nodal direction. For antinodal  $k_F$  (closed red squares),  $Z_{flux}$  is rapidly decreasing with doping, i.e.,  $Z_{flux} \rightarrow 0$  when  $\delta \rightarrow \delta_c$ , where the flux instability takes place. In order to show explicitly the anisotropy of  $\Sigma_{\it flux}$ , in Fig. 1(d), we have plotted  $Z_{flux}$  versus the FS angle  $\phi$  from  $\phi=0$  (antinodal  $k_F$ ) to  $\dot{\phi} = \pi/4$  (nodal  $k_F$ ) for  $\delta = 0.13$ . The soft d-wave mode [Fig. 1(b)], which scatters electrons on the FS with momentum transfer  $\mathbf{q} \sim (\pi, \pi)$ , is responsible for the observed anisotropy. By using  $Z_{R\lambda}$  and  $Z_{flux}$ , the total QP weight can be written as  $Z_T = 1/(Z_{R\lambda}^{-1} + Z_{flux}^{-1} - 1)$ . Blue triangles are the results for  $Z_T$  at the antinodal  $k_F$ . While for large  $\delta$ , self-energy renormalizations are dominated by  $\Sigma_{R\lambda}$ ,  $\Sigma_{flux}$  dominates near  $\delta_c$ . Results for  $Z_T$  at the nodal  $k_F$  (not shown) follow the same trend as  $Z_{R\lambda}$ , i.e., the nodal  $Z_T$  exhibits a linear behavior with slope similar to that discussed in Ref. 26.

Next we will consider the  $\Sigma_{flux}$  contribution to the spectral function  $A_{flux}(\mathbf{k},\omega)$ . Spectral functions for different  $\delta$  values near  $\delta_c$  at the antinodal  $k_F$  are presented for T=0 in Fig. 2(a). When  $\delta \rightarrow \delta_c$ , the area under the QP peak decreases (consistent with the behavior of  $Z_{flux}$ ) and spectral weight is transferred to the incoherent structure at about  $\omega \sim 0.05-0.1t$ . Figure 2(b) shows the  $\omega$  behavior of the flux scattering rate Im  $\Sigma_{flux}$  at the antinodal  $k_F$  for several  $\delta$  values near  $\delta_c$ . With

decreasing doping toward  $\delta_c$ , Im  $\Sigma_{flux}$  evolves from a Fermiliquid (FL)-like behavior ( $\sim \omega^2$ ) (see solid line for  $\delta$ =0.20) to a non-FL-like behavior ( $\sim \omega$ ) (see double-dotted-dashed line for  $\delta$ =0.13). At the same time, the structures (marked with arrows) that appear at low energy are correlated with the soft mode discussed in Fig. 1(b). Im  $\Sigma_{flux}$  at the nodal  $k_F$  (not shown) is weaker than for the antinodal  $k_F$  and, in addition, it shows a FL-like behavior for all  $\delta$  values. In summary, as observed in experiments,  $^{27,28}$  at low doping the scattering rate is strongly anisotropic on the FS, presenting a FL-like ( $\sim \omega^2$ ) behavior near the nodal  $k_F$  and a non-FL-like ( $\sim \omega$ ) behavior near the antinodal  $k_F$ . In addition, this anisotropy disappears with overdoping, where the behavior is more FL-like.

In Figs. 2(c) and 2(d), spectral functions at the antinodal  $k_F$  are presented for T=0.025 and T=0.035, respectively. For a given temperature, the intensity at the FS increases with increasing doping, showing, consistent with experiments, 17,27 a more clearly defined QP peak with overdoping. The following behavior is also interesting. For instance, for T=0.035, with decreasing doping while the peak at the Fermi level loses intensity, a broad shoulder appears at positive  $\omega$ together with an apparent gaplike (which is not a true gap) structure. As suggested by ARPES experiments, 9,19 with increasing temperature, the gaplike features seem to be filling up but are not closing (see results for  $\delta$ =0.10). Notice that for  $\delta$ =0.10, the leading edge below the FS is at  $\omega$ =-0.05twhich, using t=0.4 eV, is about 20–30 meV, thus, of the order of the observed PG value. 19 Therefore, spectral functions are strongly temperature dependent, even at temperatures much lower than the hopping t, showing broad features at the antinodal  $k_F$ . Spectral functions are nearly doping and temperature independent at the nodal  $k_F$  and show welldefined QP peaks as in experiments. 17,27 As mentioned above, at the mean-field level, when the temperature decreases, a gap opens at  $T^*$  near the hot spots. However, beyond mean field, spectral functions are very incoherent above  $T^*$ , showing that features expected to occur for  $T < T^*$  already appear for  $T > T^*$  due to self-energy renormalizations. For instance, the coherence loss when going from nodal  $k_F$  to antinodal  $k_F$  may suggest the appearance of arcs. Therefore, we think that self-energy corrections could be masking a likely abrupt change at  $T^*$  given the appearance, in agreement with observations, of a smooth crossover. In addition, it may probably be that  $T^*$  determined from the ARPES line shape is somewhat shifted from the temperature at which PG opens.

The above results are due to the doping and temperature behavior of the self-energy. In Fig. 2(e), we present results for Im  $\Sigma_{flux}$  at T=0.015 for several  $\delta$  values at the antinodal  $k_F$ . While for  $\delta$ =0.20 Im  $\Sigma_{flux}$  shows, as expected for a FL, the maximum at the Fermi level, with decreasing doping (see, for instance, double-dotted-dashed line for  $\delta$ =0.13) the maximum is shifted with respect to  $\omega$ =0. As discussed in Refs. 29 and 30, this behavior can damage the quasiparticle FL picture. For nodal  $k_F$ , the situation is FL-like, e.g., Im  $\Sigma_{flux}$  shows, for all doping values, the maximum at  $\omega$ =0, which increases with T as  $\sim T^2$ . Notice the similarities between our self-energy results in Fig. 2(e) and those discussed in Ref. 30.

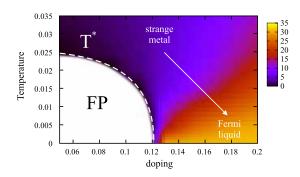


FIG. 3. (Color online)  $\omega$ =0 spectral function intensity at the antinodal  $k_F$  in the  $\delta$ -T plane.

In Fig. 3, the  $\omega$ =0 spectral function intensity at the antinodal  $k_F$  is presented in the  $\delta$ -T plane. The spectral intensity distribution suggests a crossover from a strange metal at low doping and high temperature to a FL at high doping and low temperature. Based on different arguments, recent works have proposed a similar picture.<sup>31</sup>

Before closing, let us discuss the influence of  $\Sigma_{R\lambda}$  on previous results. In Fig. 4(a), self-energy results for  $\Sigma_{R\lambda}$ ,  $\Sigma_{flux}$ , and  $\Sigma_T$ , at the antinodal  $k_F$ , are presented for  $\delta$ =0.13 and T=0.02. Im  $\Sigma_{R\lambda}$  (solid line) shows a FL-like behavior near  $\omega$ =0. The dotted-dashed line is the result for Im  $\Sigma_T$  [Eq. (1)]. While at large frequency  $\Sigma_T$  is dominated by  $\Sigma_{R\lambda}$ , properties near the FS are dominated by  $\Sigma_{flux}$ . Im  $\Sigma_T$  at the nodal  $k_F$  is very similar to Im  $\Sigma_{R\lambda}$  (solid line) because  $\Sigma_{flux}$  has no important influence on the nodal direction. In Fig. 4(b), using  $\Sigma_T$ , the total spectral functions at the nodal  $k_F$  (solid line) and at the antinodal  $k_F$  (dashed line) are presented for low  $\omega$ . For the spectral function behavior at large  $\omega$ , see Ref. 21. Although  $\Sigma_{R\lambda}$  might modify our previous results, it remains the main tendency arising from  $\Sigma_{flux}$ , i.e., the spectral functions are strongly anisotropic on the FS, losing intensity and becoming broad when going from nodal  $k_F$  to antinodal  $k_F$ .

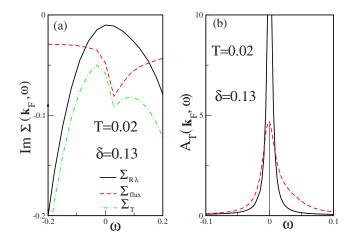


FIG. 4. (Color online) (a) Scattering rate at the antinodal  $k_F$  for  $\delta$ =0.13 and T=0.02 for  $\Sigma_{flux}$  (dashed line),  $\Sigma_{R\lambda}$  (solid line), and  $\Sigma_T$  (dotted-dashed line). (b) Total spectral function (calculated using  $\Sigma_T$ ) for  $\delta$ =0.13 and T=0.02 at the nodal  $k_F$  (solid line) and antinodal  $k_F$  (dashed line). The intensity at the nodal  $k_F$  was cut for clarity reasons.

Concluding, in the framework of the t-J model, we have computed self-energy corrections in the vicinity of the FP instability. The corresponding spectral functions are anisotropic on the FS and very incoherent near hot spots, thus they show features similar to those observed in experiments. In agreement with recent discussions (see Ref. 28 and references therein), our results show two contributions to the scattering channel. One contribution ( $\Sigma_{flux}$ ) is strongly anisotropic on the FS; the other one ( $\Sigma_{R\lambda}$ ) is very isotropic.  $\Sigma_{flux}$  dominates at low doping (near  $\delta_c$ ) and low energy, being relevant for the PG properties. In contrast,  $\Sigma_{R\lambda}$  dominates at

large doping and large  $\omega$ . In Ref. 32, by means of transport measurements, it was found that an isotropic scattering channel dominates in overdoped samples, which agrees with our predictions for  $\Sigma_{R\lambda}$ . In a recent work,<sup>33</sup> it was proposed that the high-energy features observed in ARPES<sup>34</sup> may be due to the large  $\omega$  behavior of  $\Sigma_{R\lambda}$ . Finally, our results indicate that some problems, which can be interpreted against the FP scenario, may be less serious after including self-energy renormalizations.

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- <sup>22</sup>For simplicity and without losing generality, we have considered the minimal *t-J* model. The inclusion of hopping between second, third, etc., neighbor sites produces only small quantitative but not qualitative changes.
- <sup>23</sup>This form factor is obtained after projecting the electron-boson vertex [Eq. (9) of Ref. 6] on the corresponding eigenvector for the FP instability.
- <sup>24</sup>The inclusion of a hopping between second neighbors t'/t=0.35 simply shifts  $\delta_c$  to values closer to the experimental (Ref. 16)  $\delta_c \sim 0.19$  (see Ref. 10).
- <sup>25</sup>  $\delta R$  is the fluctuation of the charge Hubbard operator  $X^{00}$  [ $X^{00}$ ] =  $\delta(1 + \delta R)$ ] associated with the number of holes.  $\delta \lambda$  is the fluctuation of the Lagrangian multiplier related to the non-double-occupancy constraint  $X^{00} + \Sigma_{\sigma} X^{\sigma\sigma} = 1$ .
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